

Trigonometry (MAC 1114)

Review Problems for Final Exam

1. Convert each of the following degree measures to radians. Leave answers as multiple of %
a) 135° b) 12° c) -315°
2. Convert each of the following degree measures to degrees.
a) $\frac{7\pi}{6}$ b) $\frac{11\pi}{3}$ a) 5 radians
3. The terminal side of angle θ in standard position goes through $(-3, -4)$. Find the values of the six trigonometric functions of θ .
4. Draw 135° in standard position. Find a point on the terminal side and then find $\sin 135^\circ$, $\cos 135^\circ$, $\tan 135^\circ$ without using a calculator.

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16. Find the domain, range, period, and amplitude of each of the following functions.

a) $y = \sin x$ b) $y = \cos x$ c) $y = \tan x$ d) $y = \csc x$ e) $y = \sec x$ f) $y = \cot x$.

17. Find the amplitude, period, and phase shift of the function, and sketch the graph of one complete period.

a) $y = -\sin 3x$ b) $y = \cos(x - \frac{\pi}{2}) + 1$

18. Evaluate the exact values of the following without a calculator.

a) $\tan(\cos^{-1}(\frac{2}{7}))$ b) $\csc(\tan^{-1}(\frac{3}{4}))$

19. True or False:

a) $\sin(-t) = -\sin t$

b) $\sec(-t) = \sec t$

c) $\tan(-t) = \tan t$

d) $\cot t = \frac{\cos t}{\sin t}$

e) $\sin t = \frac{1}{\sec t}$

f) $\sec t = \frac{\text{adjacent}}{\text{hypotenuse}}$

g) $1 + \cot^2 t = \csc^2 t$

h) $\tan t = \frac{\text{adjacent}}{\text{opposite}}$

20. Fill in the blanks without using a calculator:

a) $\tan 53^\circ = \cot \underline{\hspace{1cm}}$

b) -225° is in quadrant

c) \cos is positive in QI and

d) \tan is positive in QI and

e) $1 + \tan^2 t = \underline{\hspace{1cm}}$

f) $1 - \sin^2 t = \underline{\hspace{1cm}}$

g) $\csc t = \frac{1}{\underline{\hspace{0.5cm}}}$

Verify the following identities.

21. $\frac{1}{1 - \frac{\cos}{\cos}} = (\csc \quad \cot \quad)$

22. $\frac{\cos}{\sin} = \sin \quad \cos$

Find the missing parts of each of the following triangles.

39. $a = 39$ cm, $C = 32^\circ$, $B = 110^\circ$ 40. $b = 100$ ft, $c = 60$ ft, and $C = 28^\circ$

41. $a = 16$ m, $c = 7$ m, $B = 95^\circ$ 42. $a = 15$ ft, $b = 25$ ft, $c = 28$ ft

Find the area of each of the following triangles:

43. $a = 4$, $A = 40^\circ$, $B = 60^\circ$ 44. $a = 76.3$ ft, $b = 109$ ft, $c = 98.8$ ft

Eliminate the parameter t from each of the following parametric equations.

45. $x = 3 \sin t$ and $y = 4 \cos t$ 46. $x = \sec t$ and $y = \tan t$

47. $x = 4 \sin t - 5$ and $y = 4 \cos t - 3$ 48. $x = 5 \sin t$ and $y = -2 \sin t$

49. Write the following complex number in trigonometric form, with t between 0 and 2π

$$4\sqrt{3} - 4i$$

50. Given $z_1 = 3(\cos 60^\circ + j \sin 60^\circ)$ and $z_2 = 2(\cos 90^\circ + j \sin 90^\circ)$, find $z_1 z_2$ and z_1/z_2 .